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6		Particle						
7		Given Name	Isabel S.					
8	Corresponding	Suffix						
9	Corresponding Author	Organization	ISPA—Instituto Universitário					
10	Addition	Division						
11		Address	Rua Jardim do Tabaco, 34, Lisbon 1149-041, Portugal					
12		e-mail	isabelscampos@gmail.com					
13		Family Name	Almeida					
14		Particle						
15		Given Name	Leandro S.					
16		Suffix						
17	Author	Organization	Universidade do Minho					
18		Division	Instituto de Educação					
19		Address	Braga , Portugal					
20		e-mail						
21		Family Name	Ferreira					
22		Particle						
23		Given Name	Aristides I.					
24	A (1	Suffix						
25	Author	Organization	Instituto Universitário de Lisboa (ISCTE-IUL)					
26		Division	Business Research Unit					
27		Address	Lisboa , Portugal					
28		e-mail						
29	Author	Family Name	Martinez					

30		Particle		
31		Given Name	Luis F.	
32		Suffix		
33		Organization	Instituto Universitário de Lisboa (ISCTE-IUL)	
34		Division	Business Research Unit	
35		Address	Lisboa , Portugal	
36		e-mail		
37		Family Name	Ramalho	
38		Particle		
39		Given Name	Glória	
40		Suffix		
41	Author	Organization	ISPA—Instituto Universitário	
42		Division		
43		Address	Rua Jardim do Tabaco, 34, Lisbon 1149-041, Portugal	
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AUTHOR'S PROOF

Cognitive processes and math performance: a study with children at third grade of basic education

Isabel S. Campos • Leandro S. Almeida • Aristides I. Ferreira • Luis F. Martinez • Glória Ramalho

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Abstract The present study aims to examine the relationship between cognitive factors and 11 mathematical achievement in primary education. Participants were 103 Portuguese third 12grade students, aged 8 and 9. All participants completed a battery for working memory 13(WMTB-C), a test of general intelligence (Raven's Progressive Color Matrices), a selective 14 attention test (d2), and mathematical exercises (arithmetic story problems and measurement 15skills). Data suggested significant correlations between math performance, executive, visuo-16spatial sketchpad and g factor. Our findings suggest the importance of the cognitive factors 17in two mathematical domains considered. In consonance with the research in this area, we 18 conclude that working memory (WM) assumes an important role in different math curricular 19 achievements. 20

Keywords Mathematics performance \cdot Working memory \cdot Selective attention $\cdot g$ factor \cdot Basic education

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Introduction

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Mathematical performance is made up of a number of components such as basic knowledge25of numbers, memory for arithmetical facts, understanding of mathematical concepts, and26ability to follow problem-solving procedures (Dowker 1998). These elementary arithmetic27skills increase over time (Siegler 1988; Siegler and Shrager 1984). In the beginning, at a28basic level, children start by using fingers or other concrete references to help them with the29counting process. From these simple strategies, children move on to auditory counting,30

I. S. Campos (🖂) · G. Ramalho

ISPA—Instituto Universitário, Rua Jardim do Tabaco, 34, 1149-041 Lisbon, Portugal e-mail: isabelscampos@gmail.com

L. S. Almeida Instituto de Educação, Universidade do Minho, Braga, Portugal

starting with the addition process and continuing up to the subtraction process. Through 31 experience and improvements in working memory (WM), children are better able to 32 mentally keep track of the counting process, and thus gradually abandon the use of 33 manipulative and fingers for verbal counting (Geary 2006). 34

Although research has increased the understanding of relations between cognitive pro-35cesses and mental arithmetic, less is known about how other math domains (e.g., arithmetic 36 story problems and measurement skills) are related to cognitive capacities in the first school 37 years. The cognitive process associated to the measurement process implies the subdivision 38 of continuous quantities (such as length) in order to make them countable and comparable. 39Hence, measurement skills are complex cognitive processes associated with both number 40and arithmetic operations (Sarama and Clements 2009). Moreover, there has been some 41 discussion in the literature about the role of memory, attention, and intelligence in mathe-42matical performance and in the identification and treatment of mathematics difficulties 43(Fuchs et al. 2006; Raghubar et al. 2010). In order to clarify these questions, we aim to 44 study the association between academic performance in mathematics and some cognitive 45functions related with general intelligence (g), selective attention, and WM (CE central 46 executive, phonological loop, and visuospatial sketchpad). 47

Math performance and working memory (WM)

Some findings suggest that WM is related to a variety of mathematical outcomes when other49cognitive and academic factors are taken into account, suggesting a particular role for WM50in mathematical performance (Alloway 2009; Fuchs et al. 2005; Geary et al. 1991; Hitch and51McAuley 1991; Lee et al. 2004; Lee et al. 2009a; Passolunghi and Siegel 2004; Swanson52and Sachse-Lee 2001; Swanson and Beebe-Frankenberger 2004; Wilson and Swanson532001).54

Many studies have used the WM model of Baddeley and Hitch (1974, see also Alloway 552009; Hitch and McAuley 1991) to understand the mathematics performance of school age 56children. Baddeley (1986) defined WM as a system responsible for temporarily storing and 57manipulating information needed in the execution of complex cognitive tasks (e.g., learning, 58reasoning, and comprehension). Recently, this model has been empirically tested (Ferreira et 59al. 2011). WM consists of four components: the central executive, the phonological loop, the 60 visuospatial sketchpad, and the episodic buffer (Baddeley 2000). The CE is responsible for 61 the high-level control and coordination of information flow through WM, including tempo-62rary activation of long-term memory. It has also been linked with control processes such as 63 switching, updating, and inhibition (Baddeley 1996). The CE is supplemented by two slave 64systems specialized in information storage within specific domains. The phonological loop 65provides temporary storage for linguistic material, and the visuospatial sketchpad stores 66 information that can be represented in terms of visual or spatial content. The fourth 67 component is the episodic buffer, which is responsible for integrating information from 68 different components of WM and long-term memory into unitary episodic representations 69 70(Baddeley 2000).

Recent studies provided insight into the complexity of the relationships between WM71components and math (Bull and Scerif 2001; Lee et al. 2004; Lee et al. 2009a). For example,72the CE is assumed to be responsible for adding numbers (Logie et al. 1994), to play a crucial73role in the speed of solving mental arithmetic problems and in decision making (Baddeley741986; Logie 1993), basic calculation proficiency (Cowan et al. 2011), and contributes to75individual differences in children's mathematics achievement (Bull and Scerif 2001;76Gathercole and Pickering 2000b; Holmes and Adams 2006; Swanson and Kim 2007). The77

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phonological loop is implicated in counting (Logie and Baddeley 1987), multiplication (Lee 78and Kang 2002), and arithmetical reasoning ability (Henry and MacLean 2003). It has been 79suggested that the role of phonological WM constrains vocabulary growth during the first 80 childhood years (Gathercole and Baddeley 1993) and retains verbally coded information 81 about mathematical problems, and also supports the retrieval of mathematical facts from 82 long-term memory (Holmes and Adams 2006). Hecht et al. (2001) showed that the phono-83 logical loop was a unique predictor of mathematics achievement in primary school children. 84 A recent study by Swanson and Kim (2007) demonstrated that phonological storage was 85 uniquely related to mathematics performance in 6- to 10-year-olds. However, not all studies 86 have reported evidence in favor of this relationship. For example, Gathercole and Pickering 87 (2000b) showed that phonological loop ability was correlated with mathematics perfor-88 mance in 7- to 8-year-olds, but this association disappeared when controlling for CE ability 89 (see also Holmes and Adams 2006). Bull and Johnston (1997) demonstrated that 7-year-old 90 low mathematics achievers and high mathematics achievers differed in phonological loop 91 measures, but this difference disappeared when controlling for reading ability. 92

At the same time, research on the influence of the visuospatial sketchpad in mathematics 93 development emerged from the belief that children with mathematical disabilities showed 94impairments in visuospatial sketchpad tasks (Bull et al. 1999; Gathercole and Pickering 952000a; McLean and Hitch 1999; Van der Sluis et al. 2005). Also, some authors have reported 96 significant associations between the visuospatial sketchpad and individual differences in 97 mathematics achievement at various ages throughout primary school (Cowan et al. 2011; 98 Holmes and Adams 2006; Holmes et al. 2008; Jarvis and Gathercole 2003). Moreover, it 99 appears that the contribution of the visuospatial sketchpad in mathematics achievement 100differs as a function of age and that this contribution may be especially important during 101the initial stages of mathematics learning. For example, Rasmussen and Bisanz (2005) 102showed that the visuospatial sketchpad was associated with mathematics in preschoolers, 103but this association disappeared in first graders. Recent reports by Holmes and Adams 104(2006) and Holmes et al. (2008) indicated that the visuospatial sketchpad has a stronger 105role in 7- and 8-year-olds' mathematics performance compared with that of 9- and 10-year-106olds'. In adolescents, relations between visuospatial WM and math have been found (Kyttälä 107and Lehto 2008; Reuhkala 2001) with some differences reported for static and dynamic 108measures of visuospatial WM, depending on the particular math skill being measured (e.g., 109static related to mental arithmetic and dynamic related to geometry and word problem-110solving). In general, the findings from studies of WM components and math performance in 111 samples of elementary school children and adolescents suggest that executive and visuo-112spatial skills may be important in learning and applying new mathematical skills/concepts, 113whereas the phonological loop may come into play after a skill has been learned. By 114including separate WM dimensions, we intend to understand which dimension plays a 115higher contribution with math performance. 116

Math performance and selective attention

Selective attention—a central concept in human performance and learning—is defined as the118ability to activate and inhibit information (Hasher et al. 1999; Posner and Peterson 1990).119Several authors describe such ability as quite similar to Spearman's g factor of intelligence.120For example, on Pascual-Leone cognitive—developmental approach, the mental attention121(M) is assumed as the mental effort on problem-solving (Pascual-Leone and Baillargeon1221994). Thus, one of the most consistent findings in math disability research in recent years is123the relation between maths and attention (Bull and Johnston 1997; Fuchs et al. 2006;124

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Raghubar et al. 2009). There is some evidence that children with mathematic difficulties are125less skilled in allocating their attention resources and in monitoring the problem-solving126process (Geary et al. 1991). Deficits on selective attention affect the quality how children127initiate, inhibit, direct, and retrieve relevant information in processing different tasks (Geary128et al. 1999; Hasher et al. 1999). An example of this is comprehension of the instructions129presented on mathematical problem-solving (Jordan et al. 2003).130

Selective attention is guite similar to WM, as its measures are related to those of the CE 131 function in WM (Cantor and Engle 1993; Conway and Engle 1994; Passolunghi and Siegel 1322001; Swanson 2008). These considerations also support Swanson's (2008) findings that 133children's development of WM involves two major components: selective attention and 134storage. Differences in mathematical problem-solving may not be related directly to the 135quantity of information that can be held in memory but rather to the efficiency of inhibition 136of irrelevant information, or selective attention. Considering this, we included measures of 137WM and selective attention independently, in order to understand their separate contribu-138 tions to explain math performance. 139

Math performance and intelligence

In the psychometric tradition, general intelligence (the g factor) is defined as the use of 141deliberate mental operations to solve novel problems (i.e., tasks that cannot be performed 142automatically). These mental operations often include drawing inferences, concept formation, 143classification, generating and testing hypothesis, identifying relations, comprehending impli-144cations, problem-solving, extrapolating, and transforming information (Kane and Gray 2005; 145McGrew 2009; McGrew and Evans 2004). Recently, fluid intelligence (gf) has been assumed as 146synonymous or closely related to the general or g factor of intelligence (Ackerman et al. 2002; 147 Blair 2006) and has been explained on the basis of executive functions related to perception, 148attention, and WM (Ackerman et al. 2005; Engle et al. 1999; Kane et al. 2005; Shimamura 1492000; Smith and Jonides 1999). In fact, in the three-stratum theory of intelligence, Carroll 150(1993) distinguishes between narrow, broad, and general cognitive ability. This latter construct 151represents g factor or general intelligence, broad level embodies intermediate level abilities 152(e.g., fluid and crystallized intelligence, and processing speed), and narrow level expresses 153specific abilities such as the ones represented in the WM construct. 154

Research findings demonstrate close links between measures of WM and measures of 155 learning and intelligence (Lee et al. 2004; Swanson and Siegel 2001). It is probable that the executive system of WM (which manages a number of goals, representations, and procedures for problem-solving, which require controlled attention) acts such as the critical WM factor for fluid intelligence tasks (Fry and Hale 2000; Oberauer et al. 2003). 159

Although there is evidence in the literature that intelligence is related to math performance, several studies point out that WM scores seem to be better predictors of math achievement than measures of intelligence (Andersson 2008; Bull and Scerif 2001; Lee et al. 2004; Swanson 2004; Swanson and Beebe-Frankenberger 2004). In mathematical abilities, CE and selective attention seem to be mostly involved as a source of attention control, enabling the focusing of attention and the division of attention between concurrent tasks and attention switching.

More recently, Lee et al. (2009b) argued that WM is one of the constituent measures of 167 intelligence, and the predictive power of these two cognitive measures in math performance 168 is highly dependent on the characteristic of the tasks. To address this issue, we will adopt a 169 set of standardized tests that measures the different components of Baddeley and Hitch's 170 (1974) model. 171

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Taking into account that the three-stratum model (Carroll 1993) integrates different levels 172of cognitive abilities, we consider WM as a narrow ability, selective attention as a broad 173ability, and general intelligence as a general cognitive ability. Selective attention appears as a 174test for measuring processing speed, i.e., the ability to perform automatic cognitive tasks, 175particularly when measured under pressure to maintain focused attention (McGrew 2009). 176Considering this, the present study seeks to predict mathematical learning by certain 177178cognitive factors (WM, selective attention, and general intelligence). Also, these mathematical skills included story problems as well as other math domains, namely measurement 179skills. 180

Method

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Participants

A total of 103 third graders from two public primary schools (51.5 % males and 48.5 % 183females) from the southern region of Portugal participated in the study (88.3 % Caucasian, 18411.7 % Black). Participants' age ranged from 8 to 9 years old (approximately 99 months, 18555.3 % aged 8, while 44.7 % aged 9). The sample was randomly recruited and was not 186homogeneous in terms of race and cultural background, as is typical in Portuguese schools. 187 Moreover, from preschool to primary public school, Portuguese was the only language of 188 instruction in the classroom. All children speak Portuguese as their native language. Further 189details regarding parental occupation, education, and ethnicity were not reported. Previously, 190we carried out a preliminary study with a group of 30 third grade children (53.3 % males and 19146.7 % females) for the translation and adaptation study of WMTB-C subtests. These 192preliminary study participants were not included in the subsequent main study. In both 193studies, none of the participants had any physical, sensory, or behavioral impairment and/or 194other nationalities. Previous parental consent was obtained for each participant. 195

Instruments

Working memory (WM)

Working Memory and Test Battery for Children (WMTB-C; Pickering and Gathercole 2001) 198provide a broad-ranging assessment of WM capacities, and it is to be used with children 199between the ages of 4 and 15. It consists of nine subtests designed to tap the three main 200components of WM: the CE, the phonological loop, and the visuospatial sketchpad. For the CE 201assessment, we used listening recall, in which the children had to verify the veracity of a series 202of sentences, while remembering the last word of each sentence. In counting recall, the children 203had to count the number of dots in a series of arrays, while remembering the successive tallies of 204each array. Finally, in backward digit recall, children had to maintain the forward sequence of 205digits while recalling them in reverse order. Four subtests are designed to measure the 206phonological loop function: digit recall, word list matching, word list recall, and nonword list 207recall. In these subtests, a series of items is presented orally and children then attempt to recall 208the list in the original sequence. Finally, to assess the visuospatial sketchpad, we used block 209recall, in which a series of blocks are tapped in a three-dimensional array, and children attempt 210211to tap them in the same sequence. In mazes memory, children view a path traced by a finger through a two-dimensional maze and then attempt to recall it. A same scoring procedure was 212used in all subtests (one point for each correct answer and zero points for incorrect answers). 213

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The search of short (one-syllable) words for the Portuguese version of the WMTB-C 214 measure was identical to the English version. Some WMTB-C subtests were translated into 215Portuguese by experts in the field such as listening recall, word list recall, and word list 216matching and nonword list recall. Specific points were considered such as including simple 217and common words to be familiar for young children and guaranteeing that no one-syllable 218stimuli was repeated more than once across trials within a test. The nonsense words from 219nonword list recall were created using the same pool of sounds (phonemes) as the words 220used in the word list recall subtest. 221

This battery showed good internal consistency (Kuder-Richardson 20-KR20) for all the 222 subtests of the phonological loop: (digit recall with KR20=0.82; word list recall and word 223list matching, each of them with KR20=0.86 and nonword list recall with KR20=0.78). For 224 the visuospatial sketchpad subtests that include mazes memory and block recall, the 225coefficients were (KR20=0.75 and 0.78, respectively). Finally, the two CE subtests, listen-226ing recall and backward digit recall, revealed good internal consistency (KR20=0.80 and 2270.85, respectively); only counting recall subtest had the lowest internal consistency with 228KR20=0.70. 229

Selective attention

The d2 test (Brickenkamp and Zillmer 1998) is composed of 14 items with letters "d" and231"p" with one, two, three, or four dashes arranged either individually or in pairs above and232below the letters with a total of 658 items. Each child is given 20 s to scan each line and233mark all "d's" with two dashes. The incorrect answers were scored with zero, and the correct234items could achieve more interval values according to each child's performance. The internal235consistency was a Cronbach's value of 0.90. Also, according to Bates and Lemay (2004), d2236is a consistent and valid measure of visual scanning accuracy and speed.237

The g factor

The g factor was assessed through Raven's Progressive Color Matrices (Raven et al. 1995),239which is designed for children and consists 36 items, distributed in three sets of 12 items (A,240Ab e B). The children were asked, without a time limit, to find the missing piece in a set of241matrices that become progressively more difficult. The score for each correct answer is of242one point and for incorrect answers, zero points. The test revealed good internal consistency243(KR20=0.80).244

In order to assess math performance, we created two mathematical domains that included 245 some exercises to be solved without a time limit, so as to examine the following parameters: 246 arithmetic story problems (addition and subtraction) and measurement skills (length and 247 area). These tests were designed according to the math programme for the third year of 248 primary education with the approval of the Educational Evaluation Department (GAVE) of 249 the Portuguese Education Ministry. 250

Arithmetic story problems

This subtest has six arithmetic questions (three additions and three subtractions). Some252examples of given problems are: "In a bus there are 17 people, 4 get on. How many are there253at the moment? Or, John found 2 Euros and 60 cents on the floor. He puts the money in his254wallet. Now he has 3 Euros and 90 cents in his wallet. How much money did he have in his255wallet before he made the discovery?"256

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Measurement skills

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This section analyses children's knowledge of length and area measurement. For the measure-258ment of length, we assessed children's understanding of iteration of units and need for identical 259units of measure. We provided children with two 7-cm rulers, one marked at equal intervals, so 260that every unit was identical, and one marked at unequal intervals. Participants had to choose 261between the rulers to measure the length of a 7-cm stapler and a 9-cm book. We recorded 262children's choices, the way they measured each object, and their justification for their choices 263and methods. For area measurement, we explore children's conceptions of the unit-attribute 264relationship by eliciting their spontaneous ideas about how to find the "amount covered by" a 265square 6 cm on each side and a right isosceles triangle with a 6-cm side. We began to cover the 266cardboard square with three plastic rectangles, two plastic squares, and two plastic triangles. 267The interviewer asked the children if an answer of 7 was a good measure and they had to justify 268their answer. After that, the interviewer filled the same cardboard square with nine plastic circles 269and asked if nine was a good measure of the area. 270

We used two different scoring procedures: for arithmetic story problems, the scores were 271 one point for correct exercises and zero for incorrect answers (Vergnaud 1983); for measurement skills, the scores were zero for inexistent answers, one point when the student tried 273 to justify their choice (even when the answer was wrong), and two points when the answer 274 was correct and well justified (Lehrer and Chazan 1998). The internal consistency for 275 measurement skills and arithmetic story problems ranged from 0.72 to 0.75, respectively. 276

Procedures

Cognitive and mathematical measures were applied individually to all participants in the 278same sequence in two individual sessions which lasted about 40 min including a short pause. 279We applied the WM, g factor, and mathematical tasks without a time limit. Only the selective 280attention test was timed with a time-out of 20 s at each point. In each task, there was at least 281one practice trial before the testing phase to ensure that the children understood the task. All 282instructions regarding each task were presented orally. The order of test administration was 283held constant. We administered the WM tasks first, followed by the selective attention, the g 284factor and, lastly, the mathematical tasks. We analyzed the data with IBM SPSS 18.0 285Statistical Package. 286

Results

As a first step, we performed a correlation analysis in order to examine the relations between 288cognitive and mathematical measures. The results from the descriptive statistics and the 289correlations between specific and composite scores for the cognitive measures and mathe-290matical exercises are displayed in Table 1. Because in WMTB-C there are several measures 291292of the different WM components, we combined the scores to deal with them in the regression analysis. All of the variables were approximately normally distributed, with skewness and 293kurtosis values less than 2.0. Only measurement skills (skew=3.88) revealed a higher value, 294however, below the cutoff of 7.0 suggested by West et al. (1995). 295

All measures correlated significantly with each other. The relationship between some 296 WM components (i.e., CE, visuospatial sketchpad, and phonological loop), the selective 297 attention, g factor, and math tasks were significant, with r ranging from 0.195 to 0.779. In 298 Table 1, we find high correlation coefficients between the CE and arithmetic story problems 299

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Measures	Mean	SD	1	2	3	4	5	6
1. g factor	28.35	6.80						
2. Attention	85.18	24.86	0.349**					
3. PL	81.47	25.08	0.445^{**}	0.407^{**}				
4. VSSP	28.22	13.68	0.705^{**}	0.408^{**}	0.493**			
5. CE	80.12	26.32	0.779^{**}	0.329**	0.450^{**}	0.698^{**}		
6. Arithmetic story problems	2.98	1.57	0.653^{**}	0.401**	0.403**	0.586^{**}	0.717**	
7. Measured skills	1.85	2.12	.481**	$.279^{*}$.195*	.478**	.530**	

t1.1 **Table 1** Descriptive (mean and standard deviation) and correlation coefficients between cognitive and math measures

SD standard deviation, *PL* phonological loop, *VSSP* visuospatial sketchpad, *CE* central executive ${}^{*}p < .05$; ${}^{**}p < .01$ (two-tailed)

(r=0.717, p<.001). Lastly, the visuospatial sketchpad also showed a significant correlation 300 with arithmetic story problems (r=0.586, p<.001). 301

In order to evaluate the relationship between the cognitive variables and mathematical 302 performance, we also performed a set of multiple regression analyses (method enter) 303 considering the different math curricular areas (arithmetic story problems and measurement 304 skills) as criterion, and the CE, the visuospatial sketchpad, the phonological loop, the 305selective attention, and the g factor as predictors. We opted to introduce WM dimensions 306 in the first step, adding selective attention in the second step, and general intelligence in the 307 third step based on the three-stratum model (Carroll 1993). According to this model, WM 308 reflects narrow abilities, selective attention may be considered as a broad ability, and general 309 intelligence appears as a higher level ability. Previously, we tested regression assumptions 310with the use of collinearity statistics. All the VIF scores were below 5.0, which imply that 311 these variables do not contain redundant information (Field 2005). 312

Results of the regressions are summarized in Table 2. By using arithmetic story problems 313 as the dependent variable, we found that WM components (CE, phonological loop, and 314

	Arithmetic	e story problem	Measurement skills			
Predictor	Step 1	Step 2	Step 3	Step 1	Step 2	Step 3
(Constant)						
PL	0.072	0.022	0.019	0.036	0.006	0.002
VSSP	0.195	0.113	0.081	0.191	0.143	0.106
CE	0.531**	0.517^{**}	0.447^{**}	0.511**	0.502^{**}	0.442^{**}
Selective attention		0.224**	0.207^{*}		0.131	0.112
g factor			0.129			0.149
R^2	0.519	0.553	0.558	0.459	0.470	0.478
Adjusted R^2	0.504	0.535	0.536	0.442	0.449	0.451
ΔR^2 change in adjusted R^2	0.519**	0.034**	0.005	0.459**	0.012	0.007

t2.1 **Table 2** Summary of hierarchical regression analysis for cognitive measures predicting arithmetic story problems and measurement skills (*N*=103)

SD standard deviation, *PL* phonological loop, *VSSP* visuospatial sketchpad, *CE* central executive ${}^{*}p < .05; {}^{**}p < .01$ (two-tailed)

visuospatial sketchpad) accounted for 51.9 % of the variance when entered alone into the 315regression model (step 1), although only the CE variable is significant (β =0.531, p<.01). 316 Adding selective attention after the WM components (step 2) resulted in a significant 317 increment in R^2 , but of only 3 % of the variance. In step 3, all cognitive measures accounted 318for 55.8 % of the variance, although, the g factor did not increase R^2 significantly. 319

Considering measurement skills as the dependent variable, we found a similar pattern of 320 results to those used to predict arithmetic story problems. As shown in Table 2, WM compo-321 nents alone predict 45.9 % of the measurement skill variance. Adding all the cognitive measures 322 in the regression model (step 3) incrementally explains 47.8 % of the measurement skill 323 variance. However, the increment in R^2 is not significant, and only the CE measure is positively 324and significantly related with arithmetic story problems ($\beta = 0.442, p < .01$). 325

Overall, these results showed a significant contribution of WM in the two domains of 326 math performance. Its contribution to the shared variance is significantly higher than both 327 the g factor and selective attention. At same time, the importance of WM, and specifically 328 the CE (more than the other components), explains the large amount of variance in the 329 prediction of math results. 330

Discussion

This study explored the contribution of cognitive processes (WM components, selective 332 attention, and general intelligence) to a range of mathematical skills in elementary school 333 age children. The multiple regression analyses revealed the contribution of WM (especially 334 the CE component) to children's mathematics performance (arithmetic story problems and 335measurement skills). 336

According to our findings, the mathematical domain involved in this study, such as 337 arithmetic story problems and measurement skills (e.g., length and area), seem to require 338 executive cognitive functions, as proposed in the literature (Bull et al. 1999; Bull and Scerif 339 2001; Geary 2004; Holmes and Adams 2006; Maybery and Do 2003; Swanson 2004). For 340 example, Holmes and Adams (2006; also see Holmes et al. 2008) found that the CE 341predicted performance in several math domains (number and algebra, geometry knowledge, 342 measurement skills, data handling, and arithmetic story problems).

Also, data from this research showed that the WM CE was the most important predictor 34405 of the variance on arithmetic story problems and unique measurement skills. This seems to 345be consistent with the view that CE capacity is related to arithmetic story problems and 346different types of math problems (see for review, DeStefano and LeFevre 2004), showing the 347 relevance of executive functions in elementary learning and novel problem-solving. Recent 348 research from Meyer et al. (2010) demonstrated a higher impact on math performance of 349both CE and visuospatial sketchpad—contrarily to phonological loop. 350

Moreover, selective attention was closely related to achievement in arithmetic story 351problems. Several studies have assumed that selective attention can be observed in this 352mathematical domain (McLean and Hitch 1999; Passolunghi and Siegel 2001; Swanson and 353Beebe-Frankenberger 2004). For example, in an addition task of two- or three-digit numbers, 354some digits are selected for specific roles (e.g., first addend), while the others are held, but 355not used in the current operation. 356

In the literature, the CE and selective attention skills are thought to be involved in 357 arithmetic story problem-solving. This occurs due to the significant requirements for text 358comprehension where incoming information must be integrated with previous information 359360 maintained in WM for problem-solving. Thus, the incoming problem information must be

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examined for its relevance and then selected or inhibited for its importance in order to solve 361 that specific problem. Additionally, a number of authors claim that differences in WM span may not be related to the quantity of information that can be held in memory but rather to the efficiency of inhibition of irrelevant or no-longer-relevant information (Passolunghi et al. 1999; Passolunghi and Siegel 2001). 365

Selective attention plays an important role in WM (see Miyake and Shah 1999 for details). 366 However, in our study selective attention tasks result in lower variance when explaining math 367 performance. Our results also show that the measure of attention was not particularly strongly 368 correlated with the measure of WM. In this sense, the selective attention tasks used in this study 369 was operationalized differently from Cowan and Engle's conceptualization of WM (Miyake and 370 Shah 1999). According to Cowan's model (1999), attention was seen as "an enhancement of the 371 372 processing of information in the exclusion of other concurrent information" available (p. 63). Thus, attention is one among other mechanisms (such as memory activation and executive 373 mechanisms as well as long-term retrieval mechanisms) that contributes in processing WM 374 tasks. Engle et al. (1999) also made important contributions to the area and conceptualized WM 375 as consisting of an activated portion of long-term memory plus controlled attention. Controlled 376 attention is used to achieve activation of long-term traces to maintain activation as well as to 377 inhibit activation. Both conceptualizations of attention are far from the one used in the tasks in 378 this study. Thus, we would suggest that further studies should include attentional tasks closer to 379 the conceptualizations previously mentioned. Conceptually, d2 seems to be substantially 380 different from the more familiar tests of speed of processing used in the studies mentioned in 381 the literature. Despite these limitations, d2 is one of the most respectful tests for measuring 382selective attention. This reinforces that selective attention and WM are correlated but separate 383 constructs. Thus, selective attention plays a different role when explaining different types of 384math tasks. This stands out as a major contribution of our research. 385

Finally, let us point out that the g factor doesn't appear to be significant in the regression 386 analysis-the explained variance on math tasks is assumed by both WM and selective attention 387 measures. However, if we consider Table 1, the results suggest that g factor is correlated to both 388 arithmetic story problems and measurement skills. Considering this apparent contradiction, 389 WM seems to integrate intelligence (Ackerman et al. 2005) and selective attention (Engle et al. 3901999), namely on measurement skills tasks. On arithmetic story problems, selective attention 391has a significant effect, but below the WM effect. Thus, by activating and inhibiting the 392 cognitive processes, selective attention seems to play a significant role in solving arithmetic 393 story problems (Conway and Engle 1994; Passolunghi and Siegel 2001; Swanson 2008). 394

Regarding reliability and generalizability of these results, we should take into account 395that this study was correlational and involved a small nonrepresentative sample size of third 396 grade basic students. In order to overcome this limitation and to establish causal paths for 397 these variables, experimental studies that include other attentional variables should be 398 considered. Moreover, longitudinal studies should be carried out in order to examine the 399relation between selective attention and WM across ages. Future research should also focus 400 more specifically on different components of the CE function (inhibition, shifting, and 401 402updating) and their potential role in the development of children's story problems involving arithmetic operations and measurement skills. 403

To conclude, this paper adds to the understanding of the implications of cognitive 404 processes, especially of WM in children's maths achievement. This study also contributes 405 to a better understanding of the relation between different cognitive processes and the 406 several domains of math learning in primary education. Furthermore, the current study 407 provides additional evidence for the stronger role of the CE in different mathematic 408 competencies. 409

Cognitive processes and math performance in third grade children

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AUTHOR QUERIES

AUTHOR PLEASE ANSWER ALL QUERIES.

- Q1. "Cognitive processes and math performance in third grade children" has been provided as running head/title. Please check if appropriate.
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- Q4. "Meas. skills" has been expanded to "Measured skills". Please check if appropriate.
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