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1 **Assessing temporary speed restrictions and associated unavailability costs in railway infrastructure**

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8

9 **Highlights:**

- 10 • The occurrence of temporary speed restrictions in railway infrastructure is statistically modelled and
11 several regression models are compared;
- 12 • A Negative Binomial regression model provides a better fit than the Poisson and 'over-dispersed' Poisson
13 regression models;
- 14 • The main quality indicators for railway track geometry degradation proved to have a statistically
15 significant effect in the occurrence of temporary speed restrictions;
- 16 • The maintenance and renewal operations also have a statistically significant effect in the occurrence of
17 temporary speed restrictions;

18 **Abstract:**

19 This paper analyses the occurrence of temporary speed restrictions in railway infrastructure associated with railway
20 track geometry degradation. A negative binomial regression model is put forward to estimate the expected number
21 of temporary speed restrictions, controlling for the main quality indicators of railway track geometry degradation
22 and for the maintenance and renewal actions/decisions. The prediction of temporary speed restrictions provides a
23 quantitative way to support the assessment of unavailability costs to railway users. A case study on the Lisbon-
24 Oporto Portuguese line is explored, comparing three statistical models: the Poisson, the 'over-dispersed' Poisson
25 and the proposed negative binomial regression. Main findings suggest that the main quality indicators for railway
26 track geometry degradation are statistically significant variables, apart from the maintenance and renewal actions.
27 Finally, a discussion on the impacts of the unavailability costs associated with temporary speed restrictions is also
28 provided in a regulated railway context.

29 **Keywords:** Temporary speed restrictions; railway maintenance; statistical modelling; Negative Binomial regression;
30 unavailability costs.

31 **Background**

32 In transportation infrastructure systems, maintenance and renewal operations might cause some impacts in the
33 availability of the railway system, besides the associated costs related to these operations. One of these impacts is
34 the occurrence of temporary speed restrictions, which affect the normal operation of trains in the railway
35 infrastructure and cause unavailability costs. A main cause of the occurrence of temporary speed restrictions is the
36 degradation of railway track, namely the railway track geometry degradation. In order to study these impacts,
37 performance indicators of the railway infrastructure have to be measured and monitored [1], namely temporary
38 speed restrictions as an availability indicator. Besides, the analysis of such indicators has to take into account the
39 infrastructure influence on rail punctuality (delays), i.e. infrastructure fault datasets should be linked with
40 operational delay datasets to improve railway infrastructure management. Temporary Speed Restrictions are also
41 part of the performance indicators that regulators use to assess the infrastructure manager performance [3].
42 Moreover, the imposition of temporary speed restrictions has been found to be an influencing factor on train
43 punctuality [4]. Operating speed has also been identified as a key variable in infrastructure design consistency [5].

44 Many studies on delays in railway infrastructure have focused on quantifying the delays [6], given the occurrence of
45 a delay (e.g. a temporary speed restriction), exploring the impact of a given train delay in the network. These studies
46 do not discuss what caused the occurrence of a temporary speed restriction, and they just assume that it happens
47 and then they are interested in computing the different train delays imposed to a given network. From our
48 perspective, it seems that there is a missing link/connection/dependence between railway track geometry, the
49 maintenance and renewal actions, and the occurrence of temporary speed restrictions in the network. Moreover, in
50 any decision support system for planning maintenance and renewal actions in transportation infrastructures, the
51 assessment of unplanned impacts like the temporary speed restrictions are crucial for the definition of a
52 maintenance/renewal strategy that not only minimizes maintenance and renewal costs but also minimizes delays.

53 The past research on railway delay modelling has walked a long path, mainly focused on the quantification of train
54 delays. Several studies aimed to model train delays, considering primary delays and knock-on effects or secondary
55 delays, i.e. the propagation of delays to other trains in the network. A delay estimation methodology is put forward

56 in [7], which defines an exponential relation between travel time delay and train mix for single and double track
57 lines, validated with simulation results from a design of experiments and also with real-world delay values from a
58 sub-network existing in the Los Angeles area. Moreover, they provided an excellent review on previous research,
59 identifying two main approaches dominating the research in this topic: the analytical models and the simulation
60 models. Another approach also relied on simulation software (Rail Traffic Controller) results to fit an exponential
61 dependence with the number of trains per day to estimate average delay times for single and double track due to
62 in-service failures of different length (e.g. 1h, 3h and 5h) and associated costs [8]. They also conducted some analysis
63 on the variability of train delays for different traffic volumes. Further micro-simulation/simulation models that
64 support decisions regarding timetabling and railway operations were also explored in [9]. Another statistical
65 estimation approach to model railroad congestion delay from BNSF railway data for eight districts in the western US,
66 using multiple linear regression with an exponential functional form to explain the total train running time (i.e. the
67 free running time plus the congestion-related delay) using as independent/explaining variables: train-related and
68 track-related variables, primary and secondary-effect variables and capacity utilization effect variables [10].

69 Moreover, delays incurred by the passengers have been analysed and an overall generalized waiting cost was put
70 forward, comprising: the cost of extra stopping in the stations, the cost of extended transfer times and the cost of
71 deviating from the ideal running time supplements [11]. This approach detailed all passenger flows in train
72 connections, namely: the transfer passengers, the through passengers, the departing passengers and the arriving
73 passengers; and assigning distinct costs to each type of delay. In the same research direction, i.e. focusing in delays
74 suffered by the passengers, passenger delay models were explored, instead of the typical train delay models, in
75 which passengers are adaptive agents that may choose a different route than their planned route (assuming in the
76 most optimistic scenario that they have a complete knowledge of present and future delays in the system) [12].
77 These two contributions [11, 12] represent the most important steps towards the quantification of railway delays
78 suffered by the passengers (or freight).

79 Regarding the delays caused by the infrastructure manager, i.e. the infrastructure delays, there is a lack of published
80 references. To the best of our knowledge, the only reference discussing infrastructure delays is [13]. Delay risks

81 associated with train schedules were modelled, detailing three types of delays: track related delays, train dependent
82 delays and terminal/schedule stop delays.

83 Nevertheless, there has been little research on the impact of maintenance and renewal decisions in railway delays
84 and unavailability costs. For simplicity, let us put forward a classification for different delays, following the idea of
85 quantifying delays depending on the agent responsible for causing it, in order to frame this research work in a larger
86 research framework. The term 'agent' is used considering the vertical separation between the Infrastructure
87 Manager (IM) and the Train Operating Companies (TOC), which means that we may have as agents: the IM, the
88 different TOC and also the passengers or freights (i.e. the final users). Having said that, delays can be classified into
89 three groups:

90 i) infrastructure delays, i.e. the delays whose responsibility is assigned to the infrastructure manager;

91 ii) train operating companies delays, i.e. the delays whose responsibility is assigned to the train operating
92 companies;

93 iii) the passengers or freight delays, i.e. the delays whose responsibility is assigned to the passengers or the
94 final users.

95 This classification is particularly useful as it emphasizes the need of more research on the link between degradation
96 processes, maintenance and renewal actions of the IM's responsibility and the above-mentioned infrastructure
97 delays. Note that other railway agents that could also be integrated in this conceptual framework for a vertically
98 separated sector would be the regulator or the regulatory entity and the maintenance contractors.

99 To a certain extent, there is a parallel between this proposed delay classification and the one put forward before in
100 [13], especially in the first two groups, i.e. the infrastructure delays (or track-related delays) and the train operating
101 companies' delays (train dependent delays), respectively. However, the terminal/schedule stop delays from [13] are
102 not necessarily equal to the passenger delays as a passenger can catch a delayed train without incurring into any
103 delay impact in his/her trip.

104 Let us now focus on the infrastructure delays as they are the most relevant for IM decision-making process regarding
105 maintenance and renewal actions. There are two main types of infrastructure delays: i) the infrastructure delays due
106 to medium-/long-term changes in the maximum permissible speeds (i.e. the planned infrastructure delays) and ii)
107 the infrastructure delays due to temporary speed restrictions (i.e. the unplanned infrastructure delays).

108 Some of these delays are not even totally perceived by the passengers, by the operators and even by the regulator.
109 These delays were above defined as planned infrastructure delays because they are associated with medium-/long-
110 term downgrades of speed performance due to reductions of the maximum permissible speed. As these changes
111 immediately affect the train schedule production, they are not perceived by the other railway agents and in fact,
112 they may hide a poor performance of the IM in terms of asset management regarding maintenance and renewal
113 actions. However, the aim of this paper is to discuss solely the unplanned infrastructure delays due to temporary
114 speed restrictions and these planned infrastructure delays are left for further research, though some first steps have
115 been taken in [14] within a bi-objective optimization model for maintenance and renewal decisions.

116 The outline of this paper is as follows: this first section introduces the need to assess the occurrence of temporary
117 speed restrictions in railway infrastructure and reviewed the past research on railway delays, focusing on the delays
118 related with maintenance and renewal actions (or the 'infrastructure delays'). Afterwards, a review is provided on
119 the statistical methodology followed within the Generalized Linear Model (namely the negative binomial regression,
120 the Poisson and the 'over-dispersed' Poisson regressions), in which the different regression models are estimated
121 for our case study and compared using the Akaike Information Criterion (AIC). A context discussion on the impacts
122 of the assessment of temporary speed restrictions and associated costs in the railway regulatory framework is put
123 forward. Finally, the last section highlights the main conclusions and suggests further research in this topic.

124 **Statistical modelling of temporary speed restrictions**

125 This section explores and discusses the statistical methodology followed in this paper to predict the occurrence of
126 temporary speed restrictions in railway infrastructure within the Generalized Linear Model framework, namely using
127 the negative binomial regression model, the Poisson and the 'over-dispersed' Poisson regression models.

128 To assess the temporary speed restrictions related with rail track geometry, a database from the Portuguese IM
129 (REFER), called 'e-LVs', was analysed. This application/database compiles a series of information regarding
130 temporary speed restrictions, namely: the identification details as the line, the direction and the location; the delay
131 details as the theoretical/computed delay, the restriction speed, the maximum permissible speed, the initial and
132 final times, the motive; and other information not relevant for the following discussion.

133 Of course, many temporary speed restrictions have other motives than the ones related with the rail track subsystem
134 or related with the railway track geometry. Take for instance the example of the temporary speed restrictions due
135 to maintenance actions associated with the catenary subsystem. Those speed restrictions were not included in the
136 following assessment because only the speed restrictions related with rail track geometry condition, maintenance
137 or renewal actions were included in this analysis. In fact, IM is responsible for 20% up to 30% of the total delays in
138 the railway system, and the track system and their faults are responsible for around 3% of the total delays in the
139 railway system [1, 2].

140 Let Y be the dependent counting variable that counts the number of temporary speed restrictions that a 200-m long
141 track section suffers in a trimester period. Here, a single temporary speed restriction is any reduction of speed for
142 that 200-m long track section, i.e. when the restricted speed is lower than the maximum permissible speed for that
143 200-m long track section and for any time interval. Then, all temporary speed restrictions are summed up for a given
144 trimester, leading to the observed Y for that 200-m long track section and that trimester. Within the Generalized
145 Linear Model (GLM), two competing models are natural candidates to model the dependent variable Y : i) the Poisson
146 regression model and ii) the Negative Binomial regression model. The logarithmic function is the only link function
147 explored in both cases. A similar statistical modelling approach was also used for the assessment of
148 unplanned/corrective maintenance needs [15].

149 One of the hypotheses (or motivating ideas) to explore in the following statistical approach was related with whether
150 or not the quality indicators for rail track geometry lead to significant change in Y , i.e. the variability of the expected
151 number of temporary speed restrictions that a 200-m long track section suffers in a trimester period. Therefore, the
152 two usual indicators (for planned/preventive maintenance) were used as explaining variables: the standard deviation

153 of longitudinal level defects (SD_{LL}) and the standard deviation of horizontal alignment defects (SD_{HA}). Additionally,
154 information on all track geometry defects were also provided by the binary variables IAL (Immediate Action Limit),
155 IL (Intervention Limit) and AL (Alert Limit), so that the model could use some information on unplanned/corrective
156 maintenance needs. Finally, two additional binary covariates regarding planned maintenance and renewal
157 operations were included so that one could quantify the impact of a planned maintenance (T_p - tamping operations)
158 and of renewal operations (R_w) in the unplanned infrastructure delays (i.e. temporary speed restrictions). Regarding
159 the spatial and time spread of the sample, it refers to 14 trimesters from July 2005 up to September 2009, with a
160 total of 1358 track sections in each direction, summing up a total of 30,862 observations. All this statistical
161 information was collected within a research project for the Portuguese IM from several databases: i) inspection
162 records from EM-120 inspection vehicle, ii) infrastructure component database; iii) track component database; iv)
163 e-LVs (database dedicated to temporary speed restrictions) and v) train schedule database.

164 Table 1 details the variables considered in the model and their associated description:

165 (Table 1)

166 The Immediate Action Limits (IAL), the Intervention Limits (IL) and the Alert Limits (AL) are set by the European
167 Standard EN 13848-5 [16] for all rail track geometry defects. For further information on these rail track geometry
168 defects and their indicators, the reader is referred to [17-20], while for further details on the railway track system,
169 irregularities and variability of some physical parameters, the reader is referred to [21, 22].

170 The Poisson distribution is usually parameterized through the parameter λ and has the following probability
171 function:

$$172 \quad f(y|\lambda) = \frac{e^{-\lambda} \lambda^y}{y!} \quad (2)$$

173 For $y = 0,1,2, \dots$ and $\lambda > 0$. A Poisson distributed random variable Y has mean equal to the variance, i.e. $E[Y] =$
174 $\lambda = \mu$ and $VAR[Y] = \lambda = \mu$.

175 Within the Generalized Linear Model (GLM), in a Poisson regression model, the Poisson parameter is estimated as a
176 linear combination of covariates for each observation i , typically using a log link function, i.e. $\log(\mu_i) = \beta_0 + \beta_1 X_{i1} +$
177 $\dots + \beta_j X_{ij}$. As the Poisson model has mean equal to the variance, this model is not appropriate if there is over-
178 dispersion, i.e. when the variance is larger than the mean.

179 One simple alternative to model over-dispersed Poisson data is considering a dispersion parameter (or scale
180 parameter) ϕ in the variance expression, so that the new expression would be $VAR[Y] = \phi \cdot \mu$. This model, as an
181 extension of the Poisson regression model, is usually called the ‘over-dispersed’ Poisson model as it adds an
182 additional parameter – the scale parameter ϕ , whereas the simple Poisson regression model can be perceived as an
183 ‘over-dispersed’ Poisson model, in which the scale parameter is held equal to one ($\phi = 1$).

184 Another popular alternative to model over-dispersed counting data is the Negative Binomial model. The Negative
185 Binomial distribution is parameterized through the parameters p and r and has the following probability function:

$$186 \quad f(y|p, r) = \frac{\Gamma(y+r)}{y! \Gamma(r)} p^r (1-p)^y \quad (3)$$

187 For $y = 0, 1, 2, \dots$ and $r > 0$; $p \in (0, 1)$. A Negative Binomial random variable Y has mean $E[Y] = r \frac{1-p}{p} = \mu$ and
188 variance $VAR[Y] = r \frac{1-p}{p^2} = \mu + \frac{1}{r} \mu^2$.

189 Sometimes, the Negative Binomial regression model is parameterized in an alternative way with parameters μ and
190 r , instead of parameters p and r . The additional term $1/r$ is usually referred as the dispersion parameter or ancillary
191 parameter. The log function is also a common choice for the link function so that $\log(\mu_i) = \beta_0 + \beta_1 X_{i1} + \dots + \beta_j X_{ij}$.

192 The main difference between the over-dispersed Poisson regression model and the Negative Binomial regression
193 model is that the variance of the former is a linear function of the mean, while the variance of the latter is a quadratic
194 function of the mean [23]. The negative binomial regression model has been used in several studies related to
195 infrastructure modelling [24], from estimating transition probabilities in highway infrastructure degradation [25] to
196 hurricane-related outages in the electric power systems [26], or even in railway safety [27] and road safety [28].

197 Table 2 presents the estimated simple Poisson regression model, in which the scale parameter is held equal to 1 in
198 the estimation process of the model.

199 (Table 2)

200 First of all from the analysis of table 2, all covariates proved to be statistically significant with p-values lower than
201 1% in the Wald tests. From a 'ceteris paribus' perspective and interpreting the Incidence Rate Ratios (IRR), computed
202 as the exponential of the coefficients, i.e. e^{β_j} for each covariate j, conducting tamping maintenance operations (T_p
203 = 1) increases the expected number of speed restrictions by a multiplicative factor of 1.083, whereas conducting
204 renewal operations ($R_w = 1$) increases the expected number of speed restrictions by a multiplicative factor of 6.009.
205 Regarding covariates related with rail track geometry degradation, every unit of increase in the SD_{HA} corresponds to
206 an increase in the expected number of speed restrictions by a factor of 1.417 (i.e. 41.7% of increase); whereas every
207 unit of increase in the SD_{LL} corresponds to a decrease in the expected number of speed restrictions by a factor of
208 0.840 (i.e. 16% of decrease). Nevertheless, note that the negative sign of the coefficient relative to the SD_{LL} is not
209 intuitive and it should be interpreted as the estimated coefficient resulting from other covariates' effects.

210 Having in mind the meaning of the covariates IAL, IL and AL from table 1, one may interpret the associated
211 coefficients as the impact of all track geometry defects (besides the SD_{LL} and the SD_{HA}) in the expected number of
212 speed restrictions, but one should have in mind that $IAL=1$ implies $IL=AL=1$, whereas $IL=1$ implies $AL=1$. Therefore,
213 four cases should be interpreted: i) a track section which does not exceed any Alert Limit ($IAL=0$, $IL=0$ and $AL=0$) that
214 serves as the reference case for comparison purposes; ii) a track section which exceeds only the Alert Limits ($IAL=0$,
215 $IL=0$ and $AL=1$), corresponding to an increase of the expected number of speed restrictions by a multiplicative factor
216 of 1.395 (i.e. $\exp(\beta_{AL}) = \exp(0.333)$) comparing to the reference case; iii) a track section which exceeds the
217 Intervention Limits ($IAL=0$, $IL=1$ and $AL=1$), corresponding to an increase of the expected number of speed
218 restrictions by a multiplicative factor of 1.579 (i.e. $\exp(\beta_{AL} + \beta_{IL}) = \exp(0.333 + 0.124)$) comparing to the
219 reference case; and finally, iv) a track section which exceeds the Immediate Action Limits ($IAL=1$, $IL=1$ and $AL=1$),
220 corresponding to a decrease of the expected number of speed restrictions by a factor of 0.860 (i.e.
221 $\exp(\beta_{AL} + \beta_{IL} + \beta_{IAL}) = \exp(0.333 + 0.124 - 0.607)$) comparing to the reference case. Although the first two

222 comparisons seem intuitive, the last comparison between track sections not exceeding any limit ($IAL=IL=AL=0$) and
223 track sections exceeding all limits ($IAL=IL=AL=1$) does not seem at all intuitive. Nevertheless, the reader should again
224 have in mind that its effect must be interpreted as an estimated coefficient resulting from the combination effect of
225 other covariates rather than solely from the effect of that covariate.

226 Table 3 presents and compares two estimated models: the 'over-dispersed' Poisson and the negative binomial
227 regression models. Note that the coefficients have similar estimates under both the Poisson and negative binomial
228 models. Regarding the goodness-of-fit, AIC values indicate that the negative binomial model is considerably better
229 than the Poisson model, i.e. 62,266.37 is considerably lower than 97,601.89, indicating better relative fit of the
230 Negative Binomial regression model against the 'over-dispersed' Poisson regression model. However, a word of
231 caution must be included at this time: the AIC does not provide any indication of absolute fit. On the opposite, it
232 provides a relative indication of goodness-of-fit for competing models. Another aspect that favors the Negative
233 Binomial model against the Poisson is the considerable over-dispersion. For instance, both the Deviance/df and the
234 Pearson/df are larger than one, which clearly indicate over-dispersion in the data.

235 (Table 3)

236 From the analysis of table 3, all the covariates explored before in these models present again statistically significant
237 coefficients with p-values lower than 1% in the Wald tests, except for the Tamping (T_p) covariate ($p = 0.055$) and the
238 IL covariate ($p = 0.012$) in the 'over-dispersed' Poisson regression model, and except for the Tamping covariate ($p =$
239 0.018) in the negative binomial regression model. Moreover, note that the estimated coefficients for the initial
240 Poisson regression model (in table 2) exhibit the same value in the over-dispersed Poisson regression model (in table
241 3). Regarding the coefficients for the negative binomial regression model, they exhibit the same sign for each
242 covariate (i.e. positive or negative) as in the Poisson regression, but with slightly different values. For instance, for
243 the Tamping covariate the coefficient exhibits different values: 0.140 instead of 0.080, which would mean that
244 conducting tamping maintenance operations ($T_p = 1$) corresponds to an increase in the expected number of speed
245 restrictions by a multiplicative factor of 1.150 instead of 1.083; whereas conducting renewal operations (i.e. $R_w = 1$)
246 increases the expected number of speed restrictions by a factor of 5.748 instead of 6.009.

247 Regarding the covariates related to the rail track geometry degradation, every unit increase in the SD_{HA} would
248 correspond to an increase in the expected number of speed restrictions by a multiplicative factor of 1.822 (i.e. 82.2%
249 of increase); whereas every unit of increase in the SD_{LL} would correspond to a decrease in the expected number of
250 speed restrictions by a multiplicative factor of 0.785 (i.e. 21.5% of decrease). Again, this negative sign does not seem
251 intuitive and this coefficient should be interpreted as the estimated coefficient regarding all the other covariates'
252 effects.

253 Moreover, and following the previous strategy to interpret the coefficients from the covariates IAL, IL and AL
254 (associated with all track geometry defects or with unplanned maintenance needs), four cases are distinguished: i)
255 a track section that does not exceed any Alert Limit, i.e. $AL=0$ (which implies $IAL=IL=0$), which is the reference case;
256 ii) a track section which, at its maximum, exceeds the Alert Limits, i.e. $AL=1$ but $IAL=IL=0$, which corresponds to an
257 increase of the expected number of speed restrictions by a multiplicative factor of 1.275 (i.e. $\exp(\beta_{AL}) =$
258 $\exp(0.243)$) comparing to the reference case; iii) a track section which exceeds the Intervention Limits, i.e. $IL=AL=1$
259 but $IAL=0$, which corresponds to an increase of the expected number of speed restrictions by a multiplicative factor
260 of 1.570 (i.e. $\exp(\beta_{AL} + \beta_{IL}) = \exp(0.243 + 0.208)$) comparing to the reference case; and finally iv) a track section
261 which exceeds the Immediate Action Limits, i.e. $IAL=IL=AL=1$, corresponding to a decrease of the expected number
262 of speed restrictions by a factor of 0.861 (i.e. $\exp(\beta_{AL} + \beta_{IL} + \beta_{IAL}) = \exp(0.243 + 0.208 - 0.602)$) comparing to
263 the reference case. Again, although the first two comparisons seem intuitive, the last comparison between track
264 sections not exceeding any limit ($IAL=IL=AL=0$) and track sections exceeding all limits ($IAL=IL=AL=1$) does not seem
265 intuitive.

266 Moreover, for the 'over-dispersed' Poisson model, an additional goodness-of-fit statistic is presented: the adjusted
267 log-likelihood, which is based on the estimated scale parameter (computed based on the deviance). Note that the
268 Log-likelihood for the first Poisson regression model in table 2 and for the 'over-dispersed' Poisson regression model
269 in table 3 are the same. Finally, when the overall models are tested against the intercept model, all the three
270 investigated models are statistically significant against the intercept-only model ($p < 0.001$).

271 Although other models have not been explored in this section, the reader should consider that other distributions
272 frequently used for over-dispersed count variables are the generalized Poisson distribution and some zero-inflated
273 models. The exploration of these approaches and comparison between them and the ones here proposed is left for
274 further research.

275 According to the negative binomial regression model presented in table 3, an estimation of the expected number
276 of temporary speed restrictions ($\hat{\mu}$) for a 200-m track section in a given trimester can then be provided using the
277 following expression, depending on certain track geometry degradation indicators, i.e. the SD_{HA} (σ_{HA}) and the SD_{LL}
278 (σ_{LL}) and IAL (IAL), IL (IL) and AL (AL) defects, and also on Tamping (T_p) and Renewal (R_w) decisions:

$$279 \quad \hat{\mu} = \exp\left(\hat{\beta}_0 + \hat{\beta}_{\sigma_{HA}}\sigma_{HA} + \hat{\beta}_{\sigma_{LL}}\sigma_{LL} + \hat{\beta}_{IAL}IAL + \hat{\beta}_{IL}IL + \hat{\beta}_{AL}AL + \hat{\beta}_{T_p}T_p + \hat{\beta}_{R_w}R_w\right) \quad (4)$$

280 Values for the estimated parameters from expression 4 were presented in table 3. Figure 1 provides the expected
281 value of temporary speed restrictions ($\hat{\mu}$) for a 200-m track section in a given trimester, and contrasts it with the
282 recommended range from the European Standard EN 13848-5 for the planned maintenance criteria, i.e. the SD_{LL}
283 (1.4-2.4 mm) and the SD_{HA} (1.0-1.3 mm) defects represented by a rectangle, for the speed (S) group $120 < S < 160$
284 km/h. Figure 1 assumes that the track geometry indicators for unplanned maintenance needs (IAL, IL and AL) are
285 zero ($IAL = IL = AL = 0$), i.e. all indicators for track geometry defects are below the Alert Limits, and no tamping
286 nor renewal actions are conducted in that trimester, i.e. $T_p = R_w = 0$.

287 (Figure 1)

288 Therefore, considering the lower left corner of the rectangle, an Infrastructure Manager which sets as planned
289 criteria 1.4 and 1.0 for the SD_{LL} and SD_{HA} limits, the expected number of speed restrictions that a given track section
290 will suffer in a trimester period using expression 4: $\hat{\mu} = \exp(-0.720 + 0.600 \cdot 1.0 - 0.243 \cdot 1.4) = 0.631$; whereas
291 a strategy corresponding to the right upper corner of the rectangle (i.e. (2.4, 1.3)) leads to an expected number of
292 speed restrictions of 0.592; and a strategy corresponding to the left upper corner of the rectangle (i.e. (1.4, 1.3))
293 leads to an expected number of speed restrictions of 0.756 and finally, a strategy corresponding to the right lower

294 corner of the rectangle (i.e. (2.4, 1.0)) leads to the expected number of speed restrictions of 0.495. Similar
295 calculations can be conducted for the limits of the recommended range for each speed (S) group.

296 **Towards a more complete assessment of unavailability costs in a regulated railway industry**

297 After the introduction of the European Union (EU) directive 91/440 (EC 1991), whose aim was to 'facilitate the
298 adoption of the Community railways to the needs of the Single Market and increase their efficiency', the relation
299 between different railway stakeholders dramatically changed. The EU directive 91/440 mainly required a separation
300 between the provision of transport services and the operation of infrastructure managers by introducing separate
301 accounts between both activities and the state. It should be mentioned that though the separation of accounts was
302 compulsory, organizational and institutional separation was optional. Over the past 20 years, different policy
303 implementation took place in each EU country and, unsurprisingly, each state benefitted from different efficiency
304 effects [29].

305 Under vertical separation, the Infrastructure Manager (IM) is responsible for the maintenance and renewal actions
306 of railway infrastructure, and for operating the control and safety systems, whereas the operators are responsible
307 for the transport service for goods and/or passengers. The IM then charges a fee for the use of the railway
308 infrastructure to the operators, and the operators would sell tickets for their transport service to passengers or
309 freight (i.e. the end users). Ideally, the regulatory entity or Regulator is then responsible to ensure non-
310 discriminatory access of operators to railway infrastructure, to ensure that safety and economic regulations are
311 complied, and to provide advice to the Government/State on the asset management plans of the Infrastructure
312 Manager, particularly on its maintenance, renewal and investment plans.

313 Regarding the cost flows and necessary separate accounts, the vertical separation plan is well drawn, though its
314 implementation proved difficult as many railway companies have faced hard financial situations. Regarding the delay
315 flows, there is still a lack of understanding on this dimension, though there is a belief that from a regulatory
316 perspective, the delay dimension is crucial for performance assessment of all railway agents. For instance, the Office
317 of Rail Regulation (ORR) – the regulator for Britain's railways (one of the most active European regulators), monitors
318 the performance of railway agents through several indicators, according to its National Rail Trends (NRT) website,

319 namely: (i) temporary speed restrictions, (ii) cancellations and significant lateness, (iii) possession disruption for
320 passengers and freight trains, (iv) the punctuality performance measures and (v) passengers above capacity. These
321 five dimensions provide different performance assessment for the agents: Infrastructure Manager and Operators.
322 Note that temporary speed restrictions mainly focus in the IM performance, whereas the remaining indicators are
323 more focused in the operators' performance.

324 In fact, the Portuguese Infrastructure Manager (REFER) has been trying to implement such a system, in which REFER
325 is responsible in the operating control centers to input which agent is responsible for a given delay, as well as to
326 compute the knock-on delays assigned to that delay. In case REFER fails to assign an agent responsible, REFER is
327 considered responsible for it. This specific rule provides a clear incentive to REFER to fill that information. However,
328 as the information flow is almost completely dominated by one single agent – the Infrastructure Manager, the risk
329 that the Regulator is captured by the IM must not be neglected. Mostly because, for the case of infrastructure delays,
330 the impacts on train schedule production are immediately incorporated and are not as visible as other delays, i.e.
331 operators and passenger delays are more visible though less controllable and lead to unplanned consequences and
332 knock-on delays in the train schedules. However, if an operator does not agree that an assigned delay was its
333 responsibility, it can always protest against it to the regulator, and in many situations agreements on the split of the
334 delay consequences can be negotiated.

335 The regulatory entity as an independent safety and economic regulator monitors the performance of each agent
336 and defends the public interest. In that sense, it is extremely important to monitor all dimensions of delays,
337 especially the changes in the maximum permissible speed. Having said that, and taking for example the case of the
338 British Regulator – ORR, it seems that the changes in the maximum permissible speed have been overlooked, and
339 the regulator should take action to include them in the information flow for asset management and performance
340 monitoring.

341 Finally, in terms of detailed calculation from an economical perspective, unavailability impacts should ideally
342 distinguish each pair O-D per time period (e.g. rush hour and non-rush hour) and market segment (e.g. urban, intercity
343 and long-distance, freight) in an overall assessment of the willingness to pay for different operators and other agents

344 in the railway market. This assessment is rather complex and simplified approaches to integrate these ideas should
345 be sought in future research, particularly regarding the signals of the regulator entity on the cost quantification of
346 delays. For instance, the Portuguese regulator URF fixed a cost quantification of delays of 4 €/min for urban
347 passenger trains, and 60% of that value for intercity and long-distance trains and 5% of that value for freight trains
348 (URF 2011). Note that these values refer to costs per minute of delay per train, and not per passenger. The rationale
349 behind the setting of this values for the delays is still not transparent enough and an economic study is lacking, at
350 least for the Portuguese case.

351 **Conclusions and further research**

352 The present paper explored statistical regression approaches to model the expected number of temporary speed
353 restrictions in railway infrastructure within the Generalized Linear Framework. A negative binomial regression model
354 was considerably better than the Poisson and the 'overdispersed' Poisson regression models. The quality indicators
355 for planned maintenance, i.e. the standard deviations of longitudinal level defects and of the horizontal alignment
356 defects proved to be statistically significant predictors for the expected number of temporary speed restrictions.
357 Moreover, the variables controlling all other rail track geometry defects, i.e. IAL, IL and AL, also proved to be
358 statistically significant predictors. Finally, the maintenance (T_p) and renewal (R_w) decisions were also statistically
359 significant predictors, and exhibited Incidence Rate Ratios equal to 1.150 and 6.009, respectively. Some discussion
360 on the need to include unavailability costs associated with temporary speed restrictions was also provided.
361 Regarding further research, the final objective of the present model is the integration of the expected number of
362 temporary speed restrictions and associated delays in an objective function in order to optimize the Alert Limits that
363 trigger preventive maintenance actions, as part of a planned maintenance strategy.

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