



IDENTIFYING KEY DETERMINANTS OF HOUSING SALES AND TIME-ON-THE-MARKET (TOM) USING FUZZY COGNITIVE MAPPING

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ABSTRACT. Price and residential housing attributes have long been identified as key determinants of home sales and, as such, they can explain time-on-the-market (TOM). It is acknowledged, however, that there are other factors (or determinants) that influence home sales and TOM, which are of great importance but seldom taken into account in the appraisal process of residential real estate. Based on the use of fuzzy cognitive mapping, we propose a framework that adds value to the way that key determinants of housing sales and TOM are identified. This framework is the result of a process involving several residential real estate experts (*i.e.* appraisers and realtors), and follows a constructivist approach. Our findings suggest that the use of fuzzy cognitive maps (FCMs) allows the number of omitted determinants to be reduced and the understanding of the relationships between them to be improved. The strengths and weaknesses of our methodological framework are also discussed.

KEYWORDS: Real estate; Housing sales; Time-on-the-market; Fuzzy cognitive maps; Operational research

1. INTRODUCTION

Understanding the conditions of the residential housing market and the key attributes that determine home sales and the time taken to sell a property, broadly known as time-on-the-market (TOM) (*cf.* Cheng *et al.* 2008), is crucial in facilitating a timely and mutually beneficial sale. Price and housing attributes, in this sense, are fundamental to the success of realtors and sellers in their goal of finding a buyer, and have both long been identified as key determinants of housing sales and TOM (Leung *et al.* 2002; Cheng *et al.* 2010). It is worth noting, however, that these two factors (*i.e.* price and housing attributes) are not isolated, and that there are other determinants that influence residential real estate transactions (*cf.* Bourassa *et al.* 2003; McGreal *et al.* 2009; Hui *et al.* 2012).

Residential real estate valuation and TOM deviate due to the variety of determinants that affect them. Despite the remarkable progress of current methodologies (*e.g.* hedonic modeling,

repeated-sales methods and other mass appraisal techniques), each approach to valuation and TOM has specific limitations, requiring the clarification of a number of issues. Ferreira *et al.* (2012) argue, for example, that further developments are still required in terms of criteria identification on a more transparent (and complete) basis. Kauko (2010: 191) defends that “*academic work on defining the relevant indicators is yet speculative, due to a shortage of standard definitions and relevant data*”. From this premise, and taking into account that fuzzy cognitive mapping has proven very useful in handling this type of limitation (*cf.* Carlucci *et al.* 2013; Gavrilova *et al.* 2013), there appears considerable scope to explore its applicability in the particular context of this study.

In this paper, we use fuzzy cognitive maps (FCMs) to support the identification of key determinants of housing sales and TOM. According to Carlucci *et al.* (2013: 208), “*FCM is a well-established artificial intelligence technique, incorporating ideas from artificial neural networks and fuzzy logic, which can be effectively applied in the domain*

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of management science". This methodological framework may be used to strengthen current valuation approaches because it helps reduce the number of omitted determinants and allows the understanding of the relationships between them to be improved. Therefore, the main objective of our study is to show that the use of fuzzy cognitive mapping can give rise to a conceptually coherent and empirically valid framework to forecast TOM. Specifically, our aim is to build a cognitive map, in particular a FCM, to model, dynamically analyze and test the reciprocal influence of key determinants of housing sales and TOM. This means that we will try to identify the factors that determine TOM and their causal relationships, including their cause-effect intensities, by using data/information collected from a panel of residential real estate experts (*i.e.* professional appraisers and realtors). We have found no prior documented research applying fuzzy cognitive mapping to home valuation and TOM. As such, our study is one of the first attempts to identify key determinants of housing sales and TOM using this methodological approach. Our framework thus contributes to advance theory and empirical research on real estate, as well as on operational research.

The remainder of this paper is structured as follows. The next section provides the literature review on the key determinants of housing sales and TOM. Section 3 presents the methodological background and explores the applicability of the fuzzy cognitive mapping approach in the context of this study. Section 4 describes the process followed for the construction of our FCM, and discusses the major advantages and disadvantages of our framework. The paper finishes with concluding remarks and some lines for future research.

2. BACKGROUND ON KEY DETERMINANTS OF HOUSING SALES AND TOM

Cheng *et al.* (2010: 109) argue that "*choosing the optimal holding period is an important part of real estate investment decisions, because "when to sell" affects "whether to buy"*". In this sense, it is not surprising that significant efforts have been made to define housing values and how quickly a house can be sold (Carrillo, Pope 2012), namely because accurate valuations and TOM predictions are important for households, home sellers, buyers, investors and financial institutions that manage the underwriting risk related to housing finance. Still, these determinants of home sales are difficult to operate because residential housing usually aggre-

gates conflicting factors that interfere with market value and TOM (*cf.* Clark 1995; Zhou, Haurin 2010; Benefield *et al.* 2011).

Several techniques for estimating market value and TOM (*e.g.* hedonic modeling and other mass appraisal techniques; functional forms; non-parametric or semi-parametric regressions; spatial models that capture correlations within submarkets allowing for temporal asymmetry) have been suggested over the years (*cf.* Leung *et al.* 2002; Bourassa *et al.* 2003; Cheng *et al.* 2008; Peterson, Flanagan 2009; Carrillo, Pope 2012). However, while significant progress has occurred, these techniques are not without their flaws. In particular, they have been criticized for lack of guidance about the relationship between price and housing attributes (Bin 2004). In addition, it should be recalled that these two determinants (*i.e.* price and housing attributes) are only part of the story and that there are other factors that influence residential real estate transactions and TOM (*e.g.* individual factors; seller's search cost and strategy; market condition and maturity). Hui *et al.* (2012: 378) reinforce this assumption and refer that "*TOM is influenced by both local and national economic conditions, as well as being subject to strong seasonal effects*" (for an extensive literature that analyzes the determinants of TOM, see also Wu, Zheng 2008; McGreal *et al.* 2009; Cheng *et al.* 2008, 2010; Carrillo, Pope 2012; Vanags, Butane 2013). In this sense, "*caution [...] should be exercised [...]. Appropriate variables must be selected carefully and measured accurately*" (Bourassa *et al.* 2010: 139).

From this knowledge base, fuzzy logics (for details, see Keršulienė, Turskis 2011) may provide an important contribution in bypassing the shortcomings presented above. In particular, the use of FCM (background information is presented in the next section) can reduce the number of omitted criteria in the decision making framework and promote a better understanding of the relationships among key determinants of housing sales and TOM. Additionally, as a constructivist-based study (for details, see Ferreira *et al.* 2012), our use of FCM accepts uncertainty and allows inputs from active decision makers (*e.g.* appraisers and realtors) to be considered in the decision making framework. Due to the practical experience, technical skills and realism brought by the decision makers, the methodological proposal outlined in this paper can potentially be used by parties that invest in real estate and also by policymakers who aim to increase the efficiency of sustainable planning and forecasting in real estate. Another

important feature of our study is that it offers a perspective of complementarity rather than substitution. The next section presents the methodological background of FCM and explores the applicability of the fuzzy cognitive mapping approach in the context of this study.

3. FUZZY COGNITIVE MAPPING

Cognitive mapping has long been recognized as an important methodological approach for structuring and clarifying complex decision problems based on the human metacognitive perception (*cf.* Tolman 1948), “because cognitive maps are a useful tool for modelling the complex relationships among variables of a problem/phenomenon, even if complex” (Carlucci *et al.* 2013: 212). Gavrilova *et al.* (2013: 1758) reinforce this idea, stating that “maps as visual tools facilitate the representation and communication, support the identification and the interpretation of information, facilitate consultation and codification, and stimulate mental associations”. Although the results of these maps typically depend on the degree of involvement of the decision makers, they are usually regarded as simple, interactive and versatile. They boost discussion among the participants, allow the number of omitted criteria to be reduced, increase transparency and so significantly improve understanding of the decision problem (*cf.* Ferreira *et al.* 2012).

Kosko (1986, 1992) has been acknowledged for introducing the term FCM, as well as enhancing the power of cognitive maps (*cf.* Carlucci *et al.* 2013; Carvalho 2013). This is because the author considered fuzzy values for the criteria and fuzzy degrees of interrelationships between them. After this pioneering work, FCM has been widely applied in the analysis of different decision problems and contexts (*e.g.* Kardaras, Mentzas 1997; Tsadiras *et al.* 2003; Kok 2009; Salmeron 2009; Yaman, Polat 2009; Pappageorgiou *et al.* 2012). As pointed out by Carlucci *et al.* (2013), FCM has two particular characteristics: (1) cause-and-effect relationships between concepts/criteria follow a fuzzy logic (*i.e.* the relationship between two different criteria is simultaneously represented by a sign of positive/negative causality and by a number, ranging from -1 to 1 , that represents the intensity/influence degree of the relationship); and (2) the system is dynamic (*i.e.* it involves feedback links among the criteria, allowing temporal aspects to be considered in the decision making framework). In this sense, FCM incorporates ideas from artificial neural networks and fuzzy logic, and the typical structure of a FCM includes nodes/con-

cepts and arcs between them. Figure 1 exemplifies a FCM, where C_i stands for concept/criterion i and W_{ij} represents the influence degree of the relationship between criterion i and criterion j .

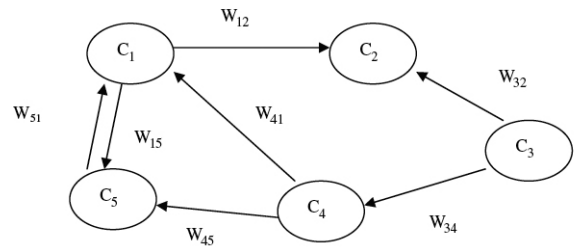


Fig. 1. Example of a typical FCM (Yaman, Polat 2009: 386)

Technically, all the values in the map can be fuzzy and, therefore, each concept has a state value A_i that can be a fuzzy value in the range between $[0, 1]$ or a bivalent logic in $\{0, 1\}$. Additionally, the weights of the arcs can be a fuzzy value within $[-1, 1]$ or a trivalent logic within $\{-1, 0, 1\}$. In this sense, it is worth noting that there are three possible types of cause-and-effect relationships between criteria/concepts: (1) *positive causality* ($W_{ij} > 0$), meaning that an increase/decrease in the value of C_i leads to an increase/decrease in the value of C_j ; (2) *negative causality* ($W_{ij} < 0$), meaning that an increase/decrease in the value of C_i leads to a decrease/increase in the value of C_j ; and (3) *null causality* ($W_{ij} = 0$), meaning no relationship between C_i and C_j (*cf.* Kim, Lee 1998; Mazlack 2009; Kok 2009; Salmeron 2009; Yaman, Polat 2009).

Behind the graphical representation, FCM has a mathematical background. Following Stylios and Groumpos (1999), Mazlack (2009) and Carlucci *et al.* (2013), there is a $1 \times n$ state vector A that includes the values of the n concepts; and a $n \times n$ weight matrix W (also known as *adjacency matrix* or *connection matrix*) that gathers the weights W_{ij} of the interconnections between the n criteria of the FCM. Although non-zero values on the main diagonal might be considered (*cf.* Kok 2009; Carvalho 2013), this matrix usually presents all entries of the main diagonal equal to zero (*i.e.* a criterion only seldom causes itself), and the value of each criterion is influenced by the values of the interconnected criteria (with the appropriate weights) and by its previous value. This means that FCM is free to interact and that, at every step of interaction, every criterion has a new value that is obtained according to formulation (1):

$$A_i^{(t+1)} = f \left(A_i^{(t)} + \sum_{\substack{j=1 \\ j \neq i}}^n A_j^{(t)} \cdot W_{ji} \right). \quad (1)$$

As explained by Mazlack (2009), $A_i^{(t+1)}$ is the activation level of criterion C_i at time $t + 1$; $A_i^{(t)}$ is the activation level of criterion C_i at time t ; $A_j^{(t)}$ is the activation level of criterion C_j at time t ; W_{ji} is the weight of the interconnection between both criteria; and f represents a threshold activation function (for further details regarding the activation function, see Stach *et al.* 2005; Papageorgiou *et al.* 2012; Salmeron 2012). From this basis, “the new state vector A_{new} is computed by multiplying the previous state vector A_{old} by the weight matrix W ” (Mazlack 2009: 6). A hypothetical example considering three concepts/criteria (*i.e.* C_1 , C_2 and C_3) is illustrated as follows:

- State vector $A_{old} = (1, 0, 1)$

$$\begin{pmatrix} 0 & 0.5 & 0.1 \\ -0.5 & 0 & 1 \\ 1 & 0.5 & 0 \end{pmatrix},$$

- Adjacency matrix $W =$

$$\begin{pmatrix} 0 & 0.5 & 0.1 \\ -0.5 & 0 & 1 \\ 1 & 0.5 & 0 \end{pmatrix},$$

- New state vector $A_{new} = A_{old} \times W = (1, 0, 1) \times 1 \times (0, 0.5, 0.1) + 0 \times (-0.5, 0, 1) + 1 \times (1, 0.5, 0) = (0, 0.5, 0.1) + (0, 0, 0) + (1, 0.5, 0) = (1, 1, 0.1)$.

The overall impact of a change in the value of one criterion can be given by A_{new} and, quoting Carlucci *et al.* (2013: 213), “the resulting transformed vector is then repeatedly multiplied by the adjacency matrix and transformed until the system converges to a fixed point. Typically it converges in less than 30 simulation time steps”. At the end of the simulation, an idea of the ranking (*i.e.* “strength of impact”) of the variables in relation to each other can be obtained, so we can see how the system is perceived in the FCM. In addition, it is possible to formulate “what-if” questions (*e.g.* what happens to a system if some of the concepts change or if new ones are introduced or removed?) and make runs to determine what state the system will go to (Carvalho 2013). All in all, “they [FCMs] have powerful and far-reaching consequences as a mathematical tool for modeling complex systems” (Mazlack 2009: 5). In light of these considerations, there is considerable scope to explore FCM applicability in the identification of key determinants of housing sales and TOM.

4. CONSTRUCTING THE FUZZY COGNITIVE MAP

The construction of our FCM took place during an intensive 6-hour group work session. As pointed

out by Yaman and Polat (2009: 387), “using a group of experts has the benefit of improving the reliability of the final model”. It should be noted, however, that “the expert panel number is quite difficult to establish and no study has been conclusive with respect to it” (Salmeron 2009: 276). In this sense, following the methodological guidelines of Eden and Ackermann (2001: 22), who state that “the consultant [*i.e.* researcher] will relate personally to a small number (say, three to ten persons)”, we involved five residential real estate experts (*i.e.* professional appraisers and realtors). These real estate experts have been developing their professional activity over the past 2–3 decades, dealing particularly with single family apartments in the Central-West region of Portugal. It is important to underline, in addition, that because our approach is process-oriented, our framework should be seen as a learning mechanism and not as an end in itself or a tool to prescribe optimal solutions. From a methodological point of view, this means that, with the necessary adjustments, the process followed can work well with a different group of decision makers and/or with a different type of residential real estate.

The session was conducted by an experienced facilitator, accompanied by two assistant technicians who were responsible for providing technical support and registering the results. Several issues were addressed in this session, including: the formulation of the “trigger question”, and the design and validation of the FCM.

4.1. Identifying concepts and quantifying relationships

To avoid misunderstandings between the team of facilitators (*i.e.* researchers) and the panel members, we started the group meeting with a kick-off presentation of the research objectives and of the basic concepts related to fuzzy cognitive mapping. Additionally, the concept of “home” was associated with “apartment” because, as already pointed out, this is the most common residential real estate in the Central-West region of the country. Given these initial clarifications, we started the operational phase of the session by asking the panel members the following trigger question: “Based on your own values and professional experience, what are the main determinants of housing sales and TOM?”. This question provided the focus for the debate/negotiation among the decision makers, and allowed the “post-its technique” to be applied.

The basis of the post-its technique consists of writing what the panel members consider as relevant concepts/criteria on post-its (*i.e.* one concept per post-it), and sticking those post-its on a large piece of paper. Supported by permanent discussion, this procedure should be repeated until the decision makers reveal satisfaction with the number and depth of the concepts identified (for further details, see Ferreira *et al.* 2014). Table 1 presents

the list of concepts/criteria obtained during the initial stage of the group meeting. It is worth noting, in addition, that the criteria identified were deeply discussed, clarified between and agreed on by the group of experts to closely reflect the determinants of TOM. Representing the group’s understanding on TOM determinants, this list is important to legitimize the results obtained and improve the face validity of the framework developed.

Table 1. List of concepts resulting from the application of the “post-its technique”

Concepts and random reference numbers		
1 Celerity	42 Competition	83 Material Conservation
2 Characteristics of the Building	43 Household Budget	84 Animals
3 Internal Characteristics (House)	44 “Haunting”	85 Storage Areas
4 External Characteristics (House)	45 Suicide	86 Storage Space
5 Exterior (Environment)	46 Rituals	87 WCs Conservation
6 Economic Factors	47 Murder	88 Sound Isolation
7 Social Stigmas	48 Drug Zone	89 Accessibility (Handicap)
8 Other Commercial Factors	49 Long Time-on-the-Market	90 Kitchen Conservation
9 Neighborhood	50 Wife	91 Disability Access
10 Several Ethnicities	51 Motivation	92 Condominium Price
11 Structure of the Building	52 Objective of the Buyer	93 Condominium Value
12 Elevator	53 Negotiation Skills	94 Gas Installations
13 Number of the Floor	54 Buyer/Seller Afinity	95 Interior Finishes
14 Noise in the Building	55 Buyer/Seller Relationship	96 Sanitaryware
15 Size of the Stairs	56 Realtor/Broker	97 Energetic Certification
16 Domestic Animals	57 Household	98 Fully Equipped Kitchen
17 Internal Access	58 Warranty	99 Sustainability
18 Internal Parking	59 Buyer Profile	100 Alarm System
19 Automatic Gates	60 Commercial Agreements	101 Dust
20 Easy Access to Parking	61 Few Apartments for Sale	102 Type of Floor
21 Porch	62 Advertising	103 Decoration
22 No Porch or Atrium	63 Number of Apartments Sold	104 Central Vacuum
23 Exterior Isolation	64 Exclusivity (+ Sale)	105 Heating
24 Conservation Degree (Exterior)	65 Exclusivity (– Sale)	106 (Other) Alarm Systems
25 Exterior Finishes	66 Promotion Channels	107 Air Conditioner
26 Type of Window Frames	67 Market “Sharks”	108 Cleaning
27 Windows with Double Glass	68 Commercial Reading	109 Sun Exposure
28 Exterior Parking	69 Council Licenses	110 Public Transports
29 Solar Panels	70 Legal Issues	111 Location
30 Swimming Pool	71 Avidity	112 View
31 Building Exterior Cleaning	72 Constructor’s Credibility	113 Neighbors
32 Price	73 Good Plumbing	114 Road Access
33 Urgency of the Sale	74 Bad Plumbing	115 Urbanization
34 Valuation	75 Number of Rooms	116 Green Spaces
35 Necessity to Sale	76 Architectural Plant	117 Mobile Network
36 Objective of the Sale	77 Size of the Rooms	118 Surroundings
37 Spread Level	78 Luminosity	119 Bus (Proximity)
38 Economic/Politic Conjuncture	79 Interior Rooms	120 “Bad” Commerce
39 Credit Access	80 Layout	121 Region/District
40 Mortgage Value	81 Humidity	122 Solar Exposition
41 “Right time” (Timing)	82 Internal Isolations	123 Street Lighting

(Continued)

Concepts and random reference numbers

(Continued)

124 Cemetery	136 Paid Parking	148 Police (Noise)
125 Garbage Pickup	137 Railways	149 Prison
126 Parking	138 Firefighters	150 Beach (Proximity)
127 Hospitals	139 Highway (Noise)	151 Recycling Areas
128 Schools	140 Pharmacy	152 Church
129 Public Services	141 Commerce	153 Industry
130 Gardens	142 Supermarkets	154 Electricity Plants
131 No Traffic	143 Industrial Zone	155 Water Treatment
132 Public Space	144 Noise	156 Sports Areas
133 Antenna/Aerial	145 Parks	157 Characteristics
134 Clear View	146 Banks (Proximity)	
135 Leisure Spaces	147 Police (Protection)	

In a second stage, the post-its were organized in a circle. This allowed pair-wise comparisons among criteria to be performed and cause-and-effect relationships to be identified. As recognized by the decision makers, this procedure was extremely important because it allowed key feedbacks to be identified in the system. Once the relationships between criteria had been identified and registered, the decision makers were asked to mark in black (continuous) or in red (discontinuous) whether they believed that there was, respectively, a positive or negative cause-and-effect relationship between the concepts. In spite of its apparent complexity, Figure 2 is illustrative of the process followed for the identification of the relationships, which are represented by arrows. It is worth noting that the resulting map was collective, negotiated between and agreed on by all.

It should be underlined that this procedure allowed decision makers to be provided with a holistic picture of the decision situation, reinforcing Kauko's (2008: 101) assumption that "*instead of isolating variables of cause of effect, it may be more relevant to give a holistic picture of the behavioural and institu-*

tional aspects of the local property market activity". In addition, as stated by one of the participating decision makers, most of determinants included in the diagram are rarely taken into account in the definition of TOM. However, the use of cognitive mapping allowed these criteria to be identified. Furthermore, adjustments (*e.g.* inclusion of new concepts) are always possible (Xue *et al.* 2010; Ferreira *et al.* 2011, 2012). This was considered extremely positive by the participating decision makers.

Aiming to simplify the visualization of the cognitive diagram presented in Figure 2, the next step consisted in the identification of clusters of criteria based on the cause-and-effect relationships previously identified. Figure 3 illustrates two different perspectives of the agreed collective map, which was constructed with the support of the *FCMapper* (<http://www.fcmapers.net>) and *Pajek* software (<http://pajek.imfm.si/doku.php>).

The next step in the construction of the FCM consisted in analyzing the intensity of the relationships identified. Figure 4 exemplifies the analysis carried out by the decision makers for one of the clusters, where the intensity of each relationship is quantified and ranges from -1 to 1 (see Kok 2009; Salmeron 2009; Yaman, Polat 2009).

This analysis was repeated for all the clusters and relationships identified in Figure 3. The decision makers were then asked to fill in a weight matrix (*i.e.* the *adjacency matrix* or *connection matrix*) containing the intensity degrees previously identified. Because the final list of TOM determinants contains 157 interlinked variables (*cf.* Table 1), the resulting matrix is a 157×157 weight matrix. Due to its considerable size, it cannot be displayed in this paper, but it is worth noting that this procedural step served to promote additional discussion on the research outputs (*i.e.* determinants of housing sales

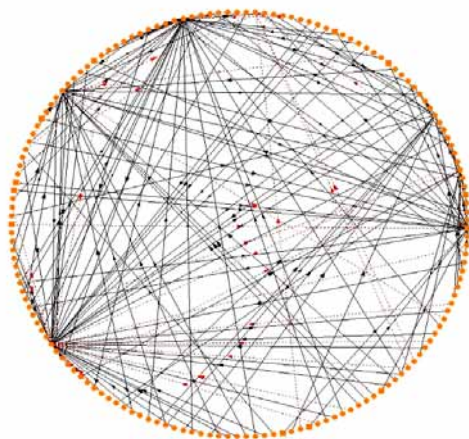


Fig. 2. Relationships between concepts

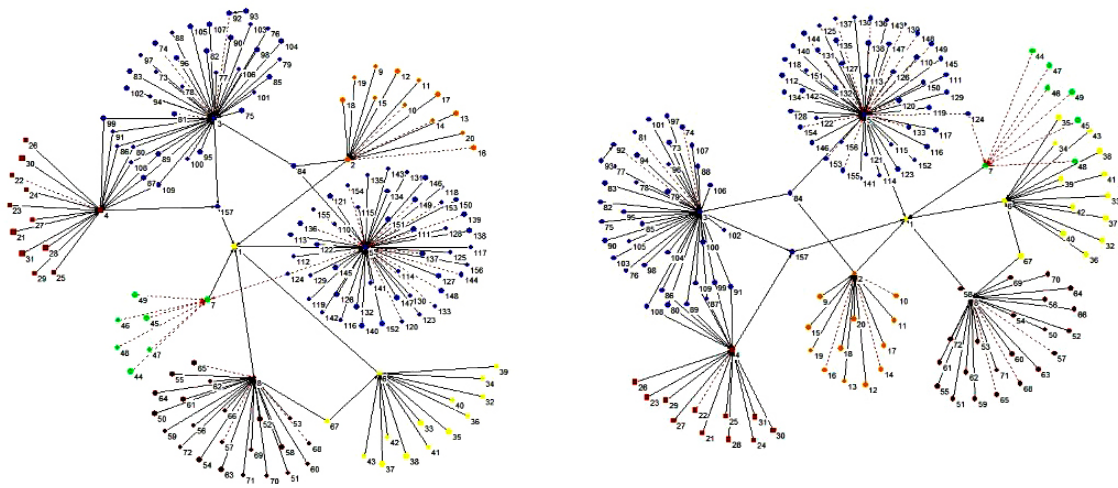


Fig. 3. Different perspectives of the agreed collective map

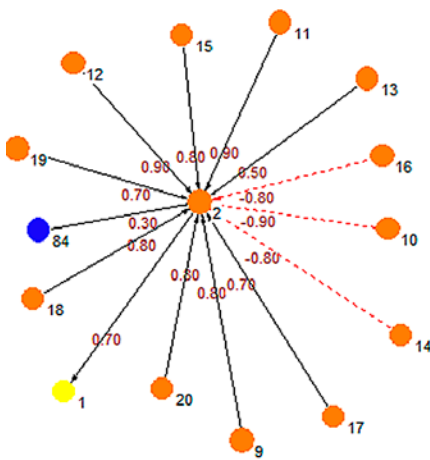


Fig. 4. Quantification of relationships

and TOM) and determine the basis for recommendations (for technical details on this procedure, see Stylios, Groumos 1999; Mazlack 2009; Salmeron 2009; Yaman, Polat 2009; Papageorgiou *et al.* 2012; Salmeron 2012; Carlucci *et al.* 2013).

4.2. Interpreting the research outputs

The final form of our FCM was discussed with the panel members, and represents the result of the negotiation and agreement reached. The form and/or content of this FCM could have been different

had the context or the participants involved been different or had the session lasted longer. However, this is an inherent characteristic of this methodology. The FCM “*should be interpreted as a tool to provide consolidated information on decision issues based on perceptions of a certain group of decision makers*” (Ferreira *et al.* 2012: 263). Furthermore, rather than a single formulaic answer, the results are aimed at encouraging discussion among experts and promoting a better understanding of the criteria associated with housing sales and TOM. In this sense, several static and dynamic analyses were carried out throughout the study. According to Carlucci *et al.* (2013: 216), “*through a proper neural network computational model, [...] what we can get is an idea of the ranking of the variables in relationship to each other according to how the system is perceived in the FCM*”. In light of this consideration, and taking into account the mathematical formulations presented in the previous section, Table 2 reveals the major determinants of housing sales and TOM that resulted from the concept interaction presented in our FCM.

It should be noted that all concepts comprised in the FCM (see Table 1) have a centrality index. However, given the high number of concepts included in our framework, Table 2 presents only the ones with

Table 2. Major determinants of housing sales and TOM [based on centrality]

Concepts	Reference	Outdegree	Indegree	Centrality
Exterior (Environment)	5	0.70	33.90	34.60
Internal Characteristics of the House	3	0.70	20.60	21.30
Other Commercial Determinants	8	0.60	16.30	16.90
External Characteristics of the House	4	1.40	12.20	13.60
Economic Determinants	6	0.90	10.60	11.50
Characteristics of the Building	2	1.60	10.40	12.00
Social Stigmas	7	0.80	5.60	6.40

the highest centrality indices. In particular, *Exterior (Environment)* and *Internal Characteristics of the House* seem to have a prominent role as determinants of housing sales and TOM, considering the respective centrality indices of 34.60 and 21.30.

These results should be treated with caution; and some of the reasons for these reservations are discussed in the next subsection. Nonetheless, it is worth highlighting that the ranking of determinants obtained in this study offers a real insight into the driving forces capable of improving real estate business performance. In addition, “*from an Artificial Intelligence perspective, FCMs are supervised learning neural systems, whereas more and more data is available to model the problem, the system becomes better at adapting itself and reaching a solution*” (Salmeron 2009: 275). Indeed, “*FCMs are simple, yet powerful tools for modeling and simulation of dynamic systems, based on domain-specific knowledge and experience*” (Papa-georgiou *et al.* 2012: 45). As such, and recalling earlier discussion, it seems safe to assume that FCMs hold great potential for strategic planning and forecasting of housing sales and TOM.

4.3. Limitations and recommendations

Kim and Lee (1998: 303) argue that “*knowledge engineering is one of the most important tasks in developing expert systems. One of the primary objectives [...] is to develop a complete, consistent and unambiguous description of the knowledge base*”. This knowledge base seems to be increasingly needed in some domains characterized as subjective and fuzzy. The appraisal process of residential real estate seems to be the case, considering that “*the real estate investment decision is not just ‘to buy, or not to buy’. It is as much ‘when to sell’ [...] the two decisions are inherently interdependent [...]*” (Cheng *et al.* 2010: 109). From this premise, the development of our FCM allowed real estate experts to: (1) identify key variables/determinants of housing sales and TOM; (2) promote discussion throughout the process, which allowed transparency and learning to be increased; and (3) provide insights about the driving forces and the key feedbacks in the system that can improve real estate business performance.

Although the system created in this study achieved encouraging results, namely as a result of the generalized satisfaction expressed by the participants, one should bear in mind that our methodological framework is not without its own limitations. Stach *et al.* (2005: 372) claim

that “*FCM development methods are far from being complete and well-defined, mainly because of the deficiencies that are present in the underlying theoretical framework [...] the development of FCM models almost always relies on human knowledge [... and] strongly depend on subjective beliefs of expert(s) from a given domain*”. Indeed, it is widely acknowledged that the conception of a cognitive map is context-dependent and, thus, subjective in nature. This context-dependence is related to the decision circumstances, participating decision makers, facilitator skills and/or session duration (Ferreira *et al.* 2012). Nonetheless, it is more than compensated by the direct involvement of experts, the amount of information discussed and by the iterative and interactive nature of the process, which allows ideas and thoughts to be shared and explored and relationships to be better understood. FCM are not a substitute for statistical approaches; however, their application by managers and decision makers can provide insights on the role of key feedbacks in the system, which might otherwise go undetected by statistical approaches alone (*cf.* Stach *et al.* 2005, 2010).

5. CONCLUSIONS

This paper aimed to identify key determinants of housing sales and TOM using fuzzy cognitive mapping. This methodological option resulted from the fact that, despite the progress achieved over the years, current available approaches to house valuation and TOM fall short to comprehensively represent the domain, as well as to enable decision makers to express their own beliefs and convictions (*cf.* Kardaras, Mentzas 1997). In this sense, our proposal resulted from the direct involvement of five real estate experts (*i.e.* professional appraisers and realtors), and assumed that the identification of key determinants of housing sales and TOM is a complex decision problem. This supported our methodological option because, according to Mazlack (2009), FCMs are neuro-fuzzy systems, which are able to incorporate experts’ knowledge and have powerful and far-reaching consequences as a mathematical tool for analysis and modeling of complex systems.

Among other achievements, our FCM allowed the participating real estate experts to: (1) identify key determinants of housing sales and TOM; (2) promote discussion throughout the process, reducing the rate of omitted criteria and increasing transparency and learning; and (3) provide insights about the driving forces and the key feed-

backs that can improve real estate business performance. In this sense, and above all, our framework provides evidence that the use of fuzzy cognitive mapping can support the identification of TOM determinants and, ultimately, has a strategic planning purpose, assisting decision makers to obtain important information about the impact of each determinant to support decisions regarding price and TOM. Obviously, FCM managerial implications go far beyond the context of this study. However, to the best of our knowledge this is one of the first attempts to identify key determinants of home sales and TOM using fuzzy cognitive mapping.

In spite of the encouraging results of this study, they are subjective in nature, because the procedures are strongly dependent on the context of analysis and the participants involved. As such, we would recommend caution in directly extrapolating these results for application in distinct contexts. That said, this is arguably more than compensated by the direct involvement of experts, the amount of information discussed and the iterative nature of the process, which allowed ideas to be shared and explored, and relationships between determinants to be better understood. In this sense, FCM has practical application for both real estate investors and policymakers who aim to increase the efficiency of sustainable planning and forecasting of housing sales and TOM.

Future research might want to work toward the improvement of our FCM-based expert system, namely in three different ways: (a) promoting its replication in other countries and with other decision makers; (b) exploring its integration within established frameworks (e.g. time series; hedonic modeling); and (c) comparing and contrasting the strengths and weaknesses of this framework to other frameworks. As already pointed out by Kok (2009: 123), “further research on the possible applications of Fuzzy Cognitive Maps is ongoing, and subsequent papers will provide a more in-depth analysis of the applicability”.

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